Welcome to CS622! Theory of Formal Languages

UMass Boston Computer Science
Instructor: Stephen Chang
Spring 2024

Today's Theme:

What's CS 622 about?

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What's this?

Interlude: CS 622 Lecture Logistics

- I expect: lecture to be interactive
 - Participation is a part of your grade
 - Also, it's the best way to learn!
- I may: call on students randomly
 - It's ok to be wrong in class! will not affect your grade
 - Also, it's the best way to learn!
- Please: tell me your name before speaking
 - Sorry in advance if I get it wrong
 - Also, it's the best way for me to learn!

What's a "language"?



What's a "language"?

```
public class Main {
  public static void main(String[] args) { object HelloWorld extends App {
     System.out.print("hello world");
                                                  println("hello world")
                                 program hello }
    <?xml version="1.0"?>
    <greeting>hello world</greeting> print *, "hello world" .model small
                                 end program hello
                                                           .stack 100h
  main = putStrLn "hello world"
                <?php echo 'hello world' ?>
                                                           msg db 'hello world$'
package main
import "fmt"
                       <?xml version="1.0"?>
func main() {
  </application> 68 65 6c 6c 6f 20 77 6f 72 6c 64 mov ax, 4C00h int 21h
createTextField("hello", 0, 0, 0, 100, 100); @echo off
hello.text = "hello world"
            IDENTIFICATION DIVISION. Imports System
PROGRAM-ID. HELLO-WORLD. Public Module modmain
PROCEDURE DIVISION. Sub Main() write('hello world'),nl.
Console.WriteLine ("hello world")
<html><body> PROCEDURE DIVISION.
SELECT 'hello world' AS hello halt;
                                   (null, "hello world"); KTHXBYE
#include <cstdio>(let ((hello-world (lambda() (display "hello world")(newline))))
int main() {
    (hello-world))
   puts("hello world"); program Helloworld; puts 'hello world'
 int main() {
                           writeln('hello world'); Print["hello world"]
                                       <cfoutput>hello world</cfoutput>
  $(function(){$('body').text('hello world');});
Transcript show: 'hello world'.public class Hello {
                                        public static void Main() {
   System.Console.WriteLine("hello world");
        #!/usr/bin/lua
              print("hello world"), document.write('hello world');
                     <% HelloWorldLabel.Text = "hello world"; %>
                    , <html><body>
  <asp:Label runat="server" id="HelloWorldLabel"></asp:Label>
                        int main (int argc, const char * argv[])
                           NSLog (@"hello world"); with Ada.Text_IO; use Ada.Text IO;
                                                     procedure Hello is
                              begin
#include <iostream> Put_Line("hello world");
                                                     end Hello;
                              int main() {
           'hello world'); cout << "hello world" << endl;
```

A Language Represents ... Computation

A programming language allows expressing and reasoning about computations

```
def f(x):
    if x > 0:
        return x +
    else:
        return x - 1
```

It's a model of computation

different???

If they are different: how can we know?

Or same???

If they are the <u>same</u>: what is a (simple) model for all of them

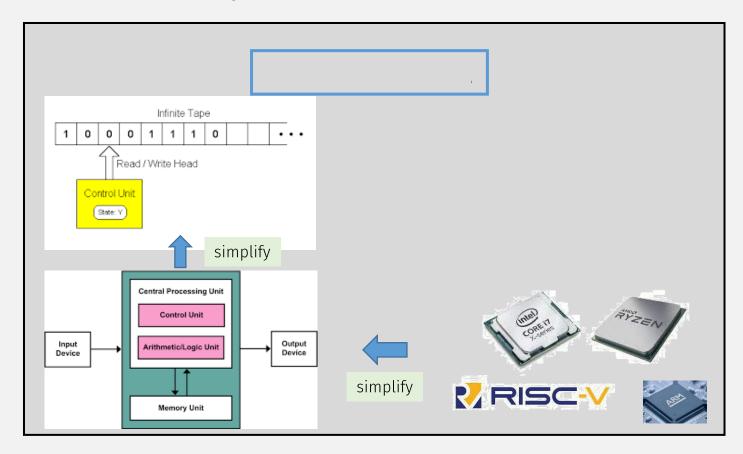




In CS 622 this semester, we will ...

- Define and study models of computation
 - models will be as simple as possible (to make them easier to study)

Models of Computation



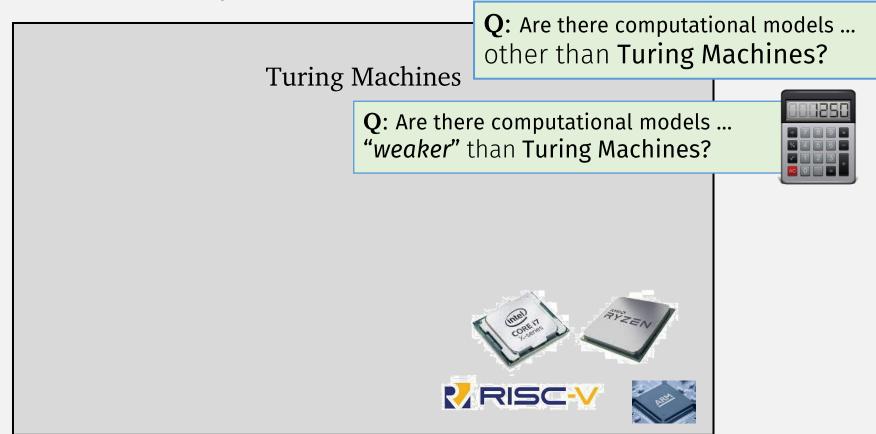
In CS 622 this semester, we will ...

- 1. <u>Define</u> and <u>study</u> models of computation
 - models will be as simple as possible (to make them easier to study)
- 2. <u>Compare</u> & <u>contrast</u> models of computation
 - which "programs" are included by a model
 - which "programs" are excluded by a model
 - overlap between models?

Models of Computation

Q: Are there computational models ... "more powerful" than Turing Machines?



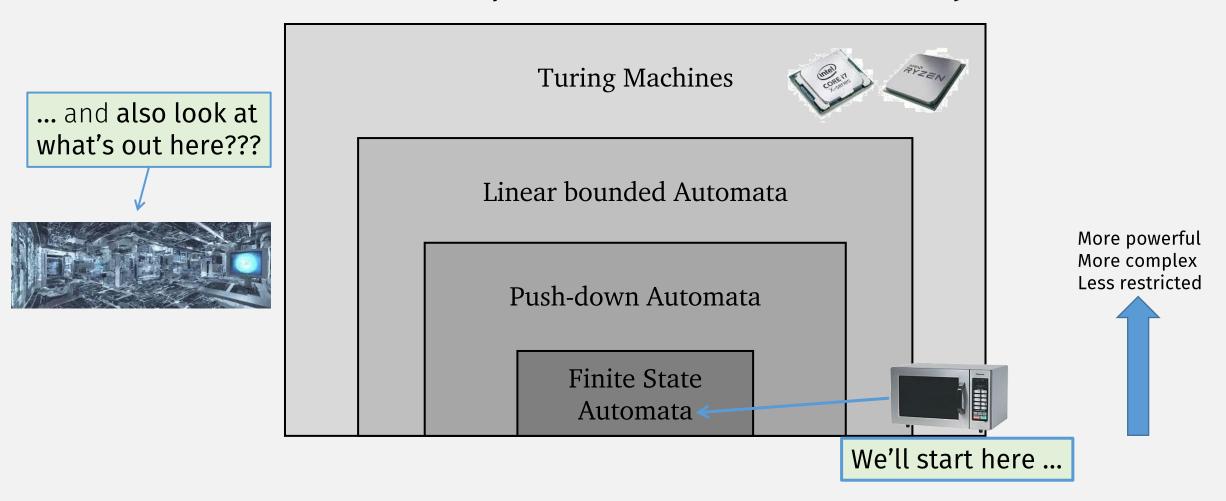


Q: What does "weaker" or "more powerful" even mean?!

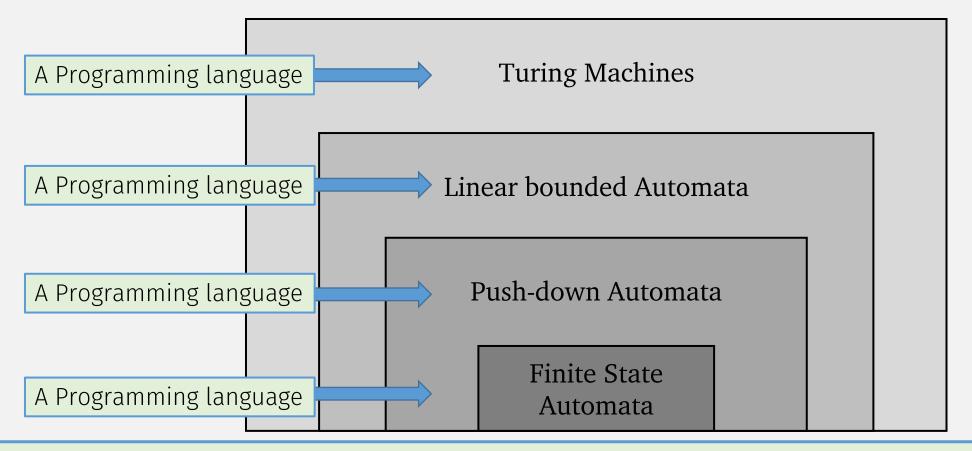
A: Yes!

Models of Computation Hierarchy

... and get to here ...



But remember ... Computation = Programs!



More powerful More complex Less restricted

Helpful analogy for this course:

- a class of machines (each rectangle above) ~ a Programming Language!
- a single machine (one thing in a rectangle) ~ a Program!

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What's this?

Welcome to CS622!

Theory of Formal Languages

UMass Boston Computer Science
or: Stephen Chang
pring 2024

"Theory" + "Formal" = math (This is a math course!)

(But programming is math too!)

Programming Is (What) Math?

Math(ematical) logic!

```
def f(x):
    if x > 0:
        return x + 1
    else:
        return x - 1

print( f(10) ) ???
```



How did you figure out the answer?



Programming = Mathematical logic!

- "logic is the foundation of all computer programming"
 - https://www.technokids.com/blog/programming/its-easy-to-improve-logical-thinking-with-programming/
- "logic is the fundamental key to becoming a good developer"
 - https://www.geeksforgeeks.org/i-cant-use-logic-in-programming-what-should-i-do/
- "Analytical skill and <u>logical reasoning</u> are prerequisites of programming because coding is effectively logical problem solving at its core"
 - https://levelup.gitconnected.com/the-secret-weapon-of-great-software-engineers-22d57f427937

Programming = Mathematical logic!

Programming Concepts

- Functions
- Variables
- If-then
- Recursion
- Strings
- Sets (and other data structures)

Math(ematical Logic) Concepts

- Functions
- Variables
- If-then (implication)
- Recursion
- Strings
- Sets (and other groupings of data)

In CS 622 this semester, we will ...

- 1. <u>Define</u> and <u>study</u> models of computation
 - models will be as simple as possible (to make them easier to study)
- 2. <u>Compare</u> & <u>contrast</u> models of computation
 - which "programs" are included by a model
 - which "programs" are excluded by a model
 - overlap between models?
- 3. Prove things about the models

You already do "Proof" when Programming

```
def f(x):
    if (x > 0) | (x < 0) | (x == 0):
        return x + 1
    else:
        return 1 / 0

print( f(10) ) ???</pre>
```





Can this function ever throw ZeroDivisionError?

How did you figure out the answer?

You did a proof!

(Let's write it out formally)

A (Mathematical) Theory Is ...

Mathematical theory

From Wikipedia, the free encyclopedia

A mathematical theory is a mathematical model of a branch of mathematics that is based on a set of axioms. It can also simultaneously be a body of knowledge (e.g., based on known axioms and definitions), and so in this sense can refer to an area of mathematical research within the established framework. [1][2]

Explanatory depth is one of the most significant theoretical virtues in mathematics. For example, set theory has the ability to systematize and explain number theory and geometry/analysis. Despite the widely logical necessity (and self-evidence) of arithmetic truths such as 1<3, 2+2=4, 6-1=5, and so on, a theory that just postulates an infinite blizzard of such truths would be inadequate. Rather an adequate theory is one in which such truths are derived from explanatorily prior axioms, such as the Peano Axioms or set theoretic axioms, which lie at the foundation of ZFC axiomatic set theory.

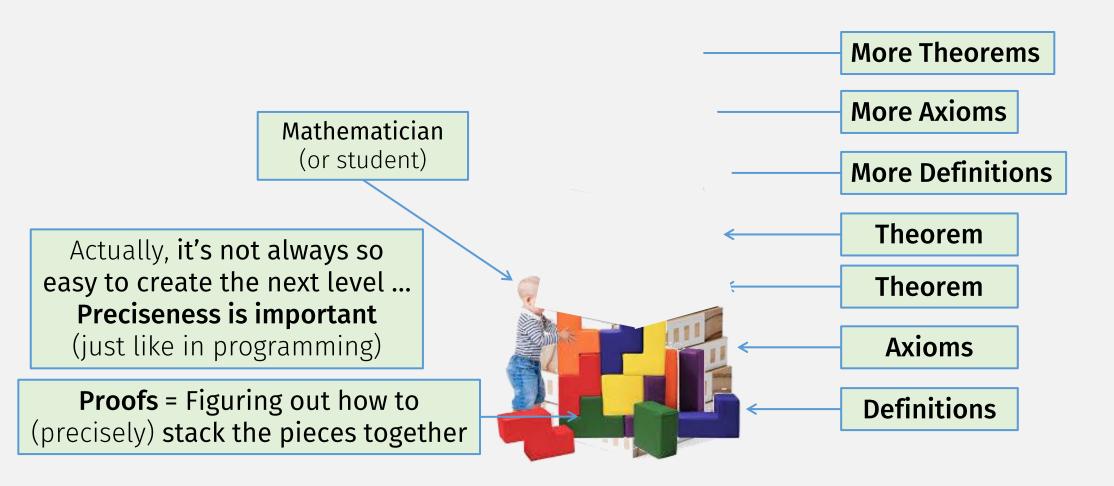
The singular accomplishment of axiomatic set theory is its ability to give a foundation for the derivation of the entirety of classical mathematics from a handful of axioms. The reason set theory is so prized is because of its explanatory depth. So a mathematical theory which just postulates an infinity of arithmetic truths without explanatory depth would not be a serious competitor to Peano arithmetic or Zermelo-Fraenkel set theory. [3][4]

... a mathematical model, i.e., axioms and definitions, of some domain, e.g. computers ...

... that **explains** (**predicts**) some real-world phenomena ...

... and can **derive** (prove) additional results (**theorems**) ...

How Mathematics Works



The "Modus Ponens" Inference Rule

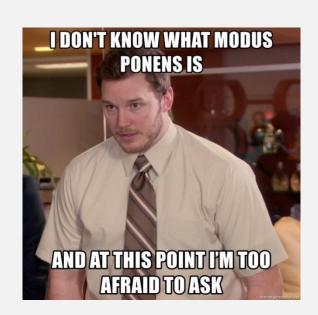
(Precisely Fitting Blocks Together)

Premises (if we can show these statements are true)

- If P then Q
- P is TRUE

Conclusion (then we can say that this is also true)

Q must also be TRUE



Kinds of Mathematical Proof

Deductive Proof

- Start with: known facts and statements
- Use: logical inference rules (like modus ponens) to prove new facts and statements