UMass Boston Computer Science

CS450 High Level Languages (section 2)

Interpreting Recursion, with Mutation!

Monday, December 4, 2023

Logistics

- HW 8 in
  - ~~due: Sun 12/3 11:59 pm EST~~
  - ~~due: Mon 12/4 11:59 am EST~~

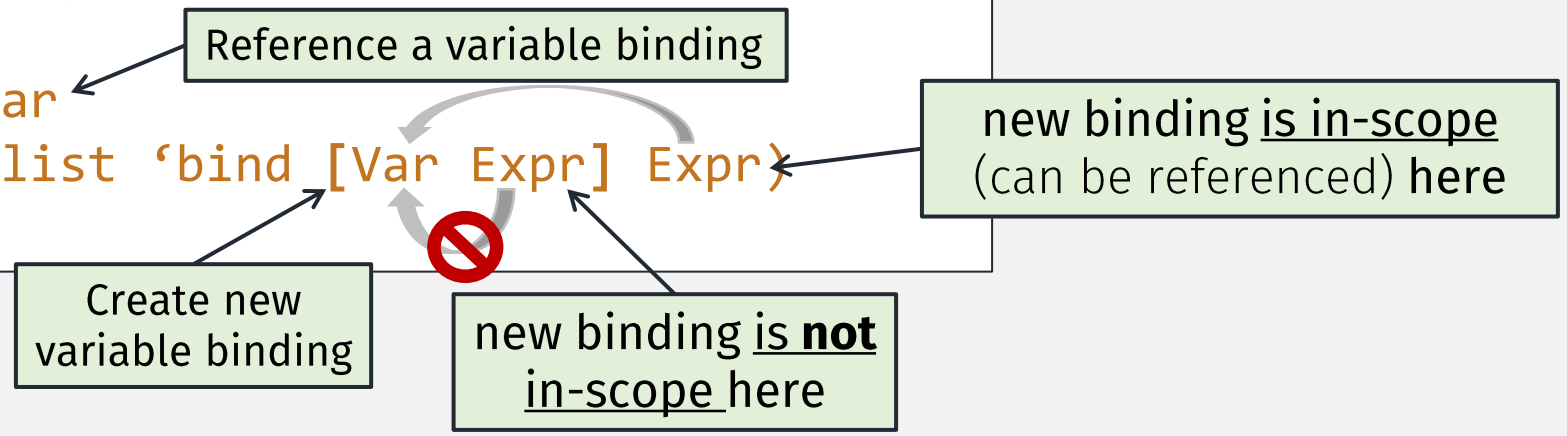
- HW 9 out
  - due: Sun 12/10 11:59 pm EST

Last Time

"bind" in "CS450JS" Lang

```
;; A Variable (Var) is a Symbol
```

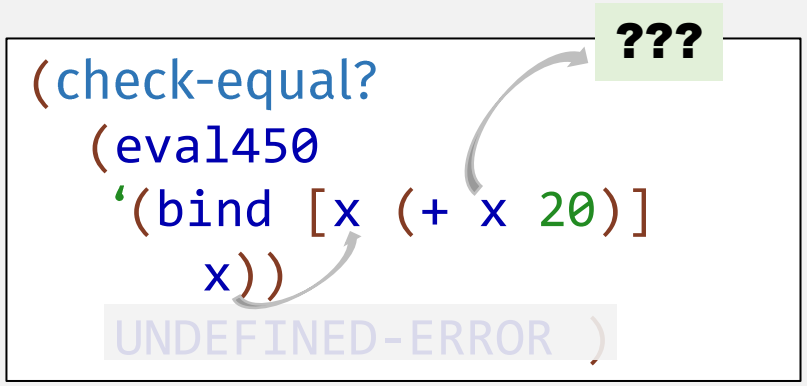
```
;; A 450jsExpr (Expr) is one of:
;; …
;; - Var
;; - (list 'bind [Var Expr] Expr)
;; …
```



Last Time

`bind` examples

```
;; A 450jsExpr (Expr) is one of:
;; …
;; - Var
;; - (list 'bind [Var Expr] Expr)
;; …
```



bind examples, with functions

```
;; A 450jsExpr (Expr) is one of:
;; …
;; - Var
;; - (list 'bind [Var Expr] Expr)
;;   (list 'fn List<Var> Expr)
;;   (cons Expr List<Expr>)
;; …
```

"lambda" function

function

arguments

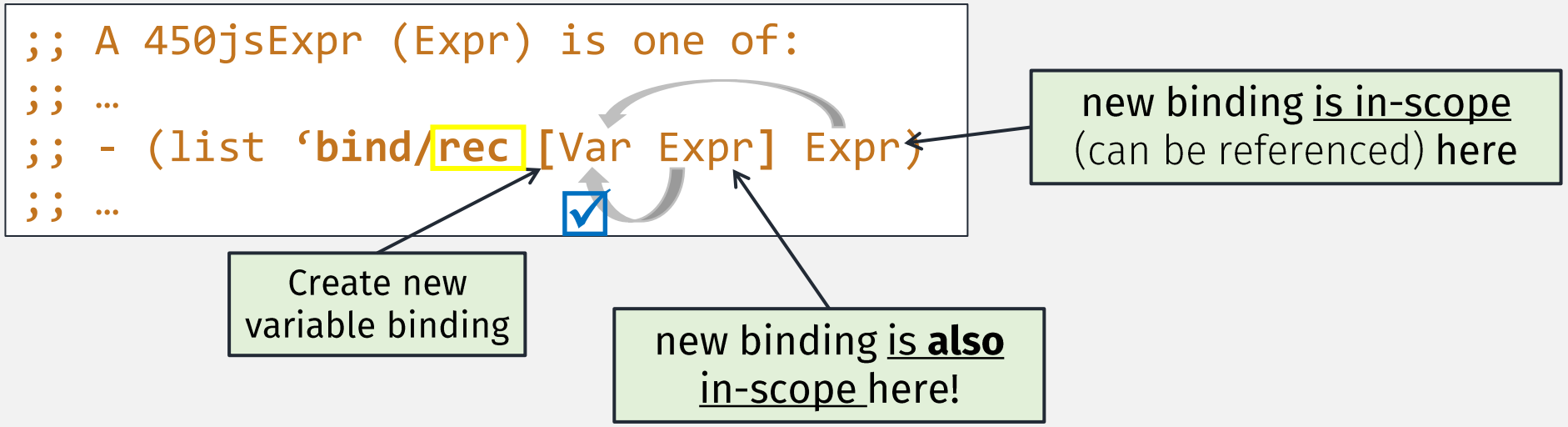
function call

```
(check-equal?
  (eval450
   '(bind [f (fn (x) (+ x 4))]
      (f 6)))
   10 )
```

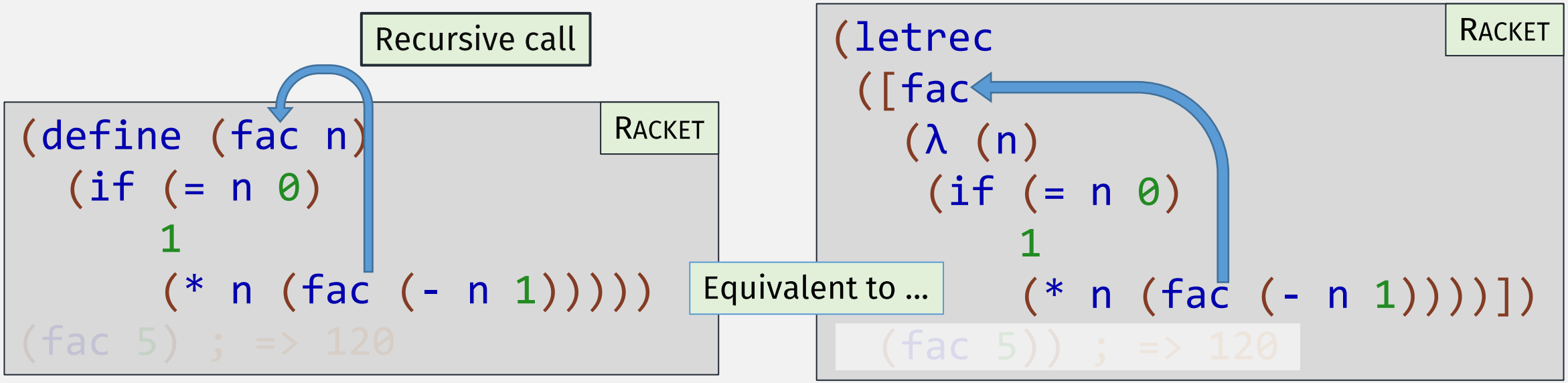
f not in-scope here
(function can't be recursive!)

“bind/rec” in “CS450JS” Lang

```
;; A 450jsExpr (Expr) is one of:
;; …
;; - (list 'bind/rec [Var Expr] Expr)
;; …
```



Racket recursive function examples



`bind/rec` examples

```
;; A 450jsExpr (Expr) is one of:
;; …
;; - (list 'bind/rec [Var Expr] Expr)
;; - (list 'iffy Expr Expr Expr)
;; …
```

JS "truthy" if (hw7)

RACKET

```
(letrec
 ([fac
   (λ (n)
    (if (= n 0)
        1
        (* n (fac (- n 1)))))])
  (fac 5)) ; => 120
```

Equivalent to …

CS450JSLANG

```
(bind/rec
 [fac
  (fn (n)
    (iffy n
        (* n (fac (- n 1)))
        1))]
  (fac 5)) ; => 120
```

Zero is "truthy" false (hw7)

Running **`bind/rec`** programs

```
;; A 450jsExpr (Expr) is one of:
;; …
;; - (list 'bind/rec [Var Expr] Expr)
;; …
```

parse

```
;; A 450jsAST (AST) is one of:
;; …
;; - (recb Symbol AST AST)
;; …
(struct recb [var expr body])
```

run

```
;; A 450jsResult (Result) is a:
;; - …
```

Running **bind/rec** programs

TEMPLATE ?

```
;; run: AST -> Result
;; Computes result of
running CS450js AST
```

```
;; A 450jsAST (AST) is one of:
;; …
;; - (recb Symbol AST AST)
;; …
(struct recb [var expr body])
```

run

```
;; A 450jsResult (Result) is a:
;; - …
```

Running **bind/rec**

TEMPLATE : extract pieces

```
;; run: AST -> Result
(define (run p)

  (define (run/e p env)
    (match p
      …
     [(recb x e body) ?? x   ??      e       ??      body ))))]
      … ))
 (run/e p  ???  ))
```

```
;; A 450jsAST (AST) is one of:
;; …
;; - (recb Symbol AST AST)
;; …
(struct recb [var expr body])
```

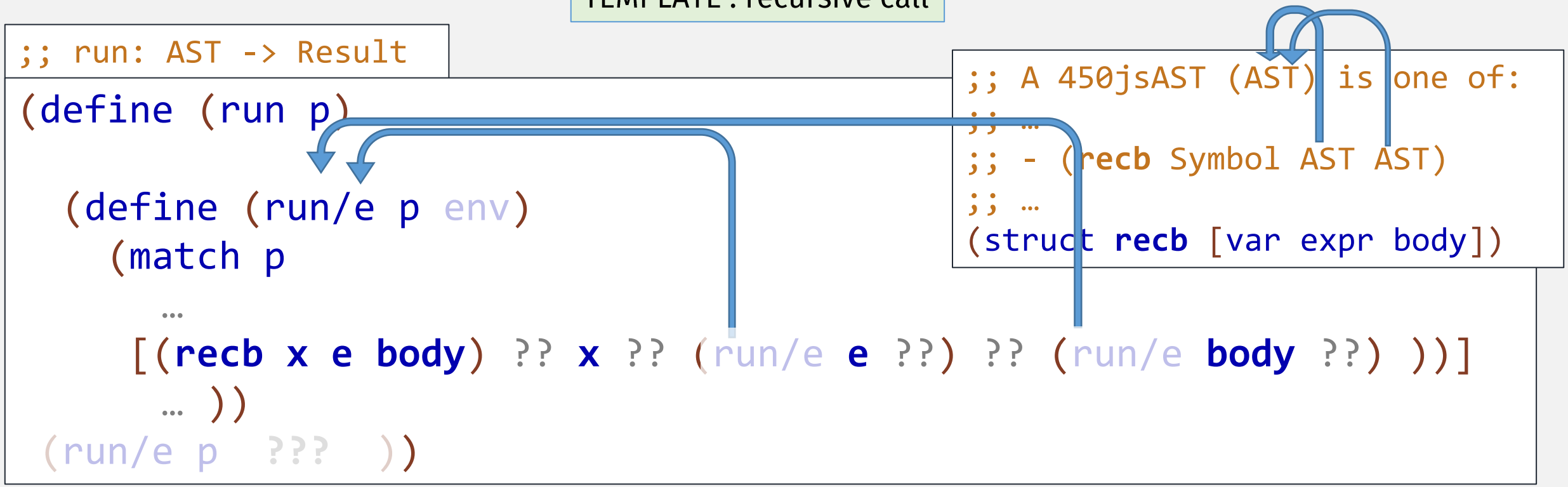
Running **bind/rec**

TEMPLATE : recursive call

```
;; run: AST -> Result
(define (run p)

  (define (run/e p env)
    (match p
      …
     [(recb x e body) ?? x ?? (run/e e ??) ?? (run/e body ??) ))]
      … ))
 (run/e p  ???  ))
```

```
;; A 450jsAST (AST) is one of:
;; …
;; - (recb Symbol AST AST)
;; …
(struct recb [var expr body])
```



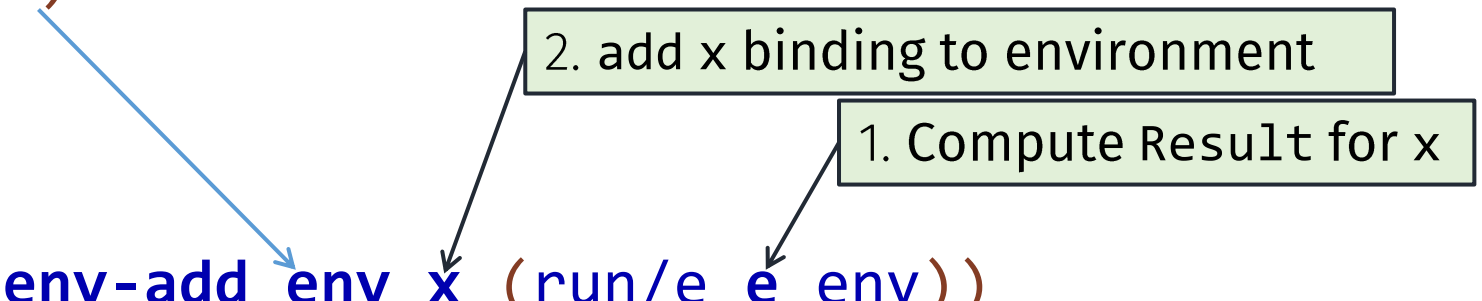
Running **`bind/rec`**, using environment

```
;; run: AST -> Result
(define (run p)
  ;; accumulator env : Environment
  (define (run/e p env)
    (match p
      …
      [(recb x e body) ?? x ?? (run/e e ??) ?? (run/e body ??) ))]
      … ))
 (run/e p INIT-ENV ))
```

```
;; An Environment (Env) is one of:
;; - empty
;; - (cons (list Var Result) Env)
```

Running **`bind/rec`**, using environment

```
;; run: AST -> Result
(define (run p)
  ;; accumulator env : Environment
  (define (run/e p env)
    (match p
      …
     [(recb x e body)
      (define env/x (env-add env x (run/e e env))
      (run/e body env/x)]
      … ))
 (run/e p INIT-ENV ))
```



Running **bind/rec**, using environment

CS450JSLANG

```
(bind/rec
 [fac
  (fn (n)
    (iffy n
          (* n (fac (- n 1)))
          1))]
  (fac 5)) ; => 120
```

```
;; run: AST -> Result
(define (run p)
  ;; accumulator env : Environment
  (define (run/e p env)
    (match p
      …
      [(recb x e body)
       (define env/x (env-add env x (run/e e env/x)))
       (run/e body env/x)]
      … ))
  (run/e p INIT-ENV))
```

??? This is circular! (no base case)

env/x

Compute body with x in-scope

PROBLEM:
x should be in-scope here too!

Interlude: Mutation

- **Mutating** a variable means to change its value after it is defined

```
(define x 3)
(display x) ; 3
(set! x 5) ; mutate x
(display x) ; 5
```

Interlude: Mutation

- **Mutating** a variable means to change its value after it is defined

- **Mutation** should be rarely used, only in appropriate situations

Interlude: Mutation

- **Mutating** a variable means to change its value after it is defined

- **Mutation** should be <u>rarely used</u>, only in appropriate situations

> *Item 3: Use const whenever possible.*
>
> **Effective C++**, Scott Meyers, 2005.

Item 15, "Minimize mutability. **Joshua Bloch** Author, Effective Java, Second Edition

Joshua Bloch, Google's chief Java architect, is a former Distinguished Engineer at Sun Microsystems, where he led the design and implementation of numerous Java platform features, including JDK 5.0 language enhancements and the award-winning Java Collections Framework.

Immutability makes <u>code easier to read</u> and understand

Item 15 tells you to keep the state space of each object as simple as possible. If an object is immutable, it can be in only one state, and you win big. You never have to worry about what state the object is in, and you can share it freely, with no need for synchronization. If you can't make an object immutable, at least minimize the amount of mutation that is possible. This makes it easier to use the object correctly.

Interlude: Mutation

- **Mutating** a variable means to change its value after it is defined

- **Mutation** should be rarely used, only in appropriate situations

Because:

- It **makes code more difficult to read**
  - (just like inheritance and dynamic scope)
- It **violates "Separation of concerns"**

```
(define x 3)
(do-something x) ; mutate x??
(display x) ; ???
```

Interlude: Mutation

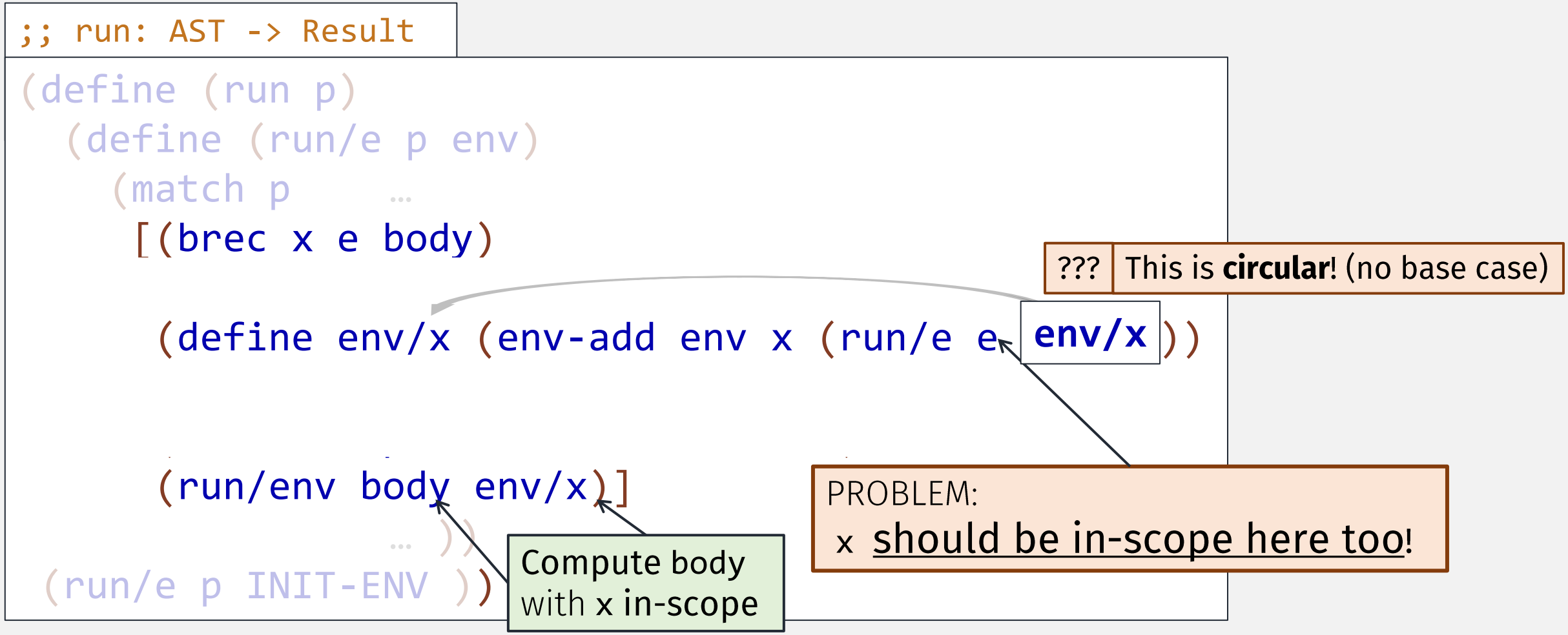
- **Mutating** a variable means to change its value after it is defined

- **Mutation** should be rarely used

When is using **mutation** ok:

- Performance
  - Typically **not using high-level languages!** (**OS, AAA game** i.e., not this class!)
  - Beware of **pre-mature optimization!**
- **Shared state** (in distributed programs)
  - Beware of **race conditions and deadlock!**
- **Circular data structures** (e.g., circular lists)

Running **`bind/rec`**, recursive environment items



Running **bind/rec**, recursive environment items

```
;; run: AST -> Result
(define (run p)
  (define (run/e p env)
    (match p     …
     [(brec x e body)
      (define placeholder (box CIRCULAR-ERROR))
      (define env/x (env-add env x placeholder))

      (run/env body env/x)]
                …  ))
 (run/e p INIT-ENV ))
```

Creates **mutable box**
Makes mutation explicit

```
;; A 450jsResult is a:
;; - Number
;; - FunctionResult
;; - 450jsErrorResult
```

```
;; A 450jsErrorResult is a:
;; - UNDEFINED-ERROR
;; - ARITY-ERROR
;; - CIRCULAR-ERROR
```

Running **`bind/rec`**, recursive environment items

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(define (run p)
  (define (run/e p env)
    (match p    …
     [(brec x e body)
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      (define env/x (env-add env x placeholder))

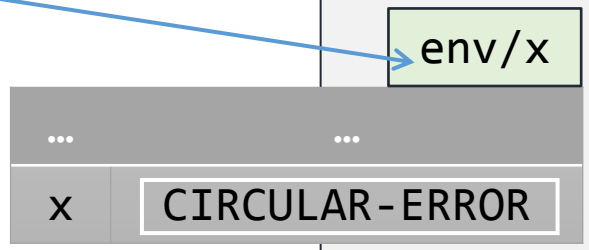

      (run/env body env/x)]
                …  ))
 (run/e p INIT-ENV ))
```

```
;; An Environment (OLD) (Env) is one of:
;; - empty                    ???
;; - (cons (list Var 450jsResult) Env)
```

(how would env-add and env-lookup need to change?)

```
;; An Environment (Env) is a: List<EnvVal>
```

```
;; An EnvVal is one of:
;; - 450jsResult
;; - Box<450jsResult>
```



Running **`bind/rec`**, recursive environment items

```
(bind/rec [f f] f)
 ; => CIRCULAR-ERROR
```

CS450JSLANG

```
;; run: AST -> Result
(define (run p)
  (define (run/e p env)
    (match p     …
     [(brec x e body)
      (define placeholder (box CIRCULAR-ERROR))
      (define env/x (env-add env x placeholder))
      (define x-result (run/env e env/x))

      (run/env body env/x)]
                 … ))
 (run/e p INIT-ENV ))
```

Non-function, circular recursive references (no base case) produce error results!

Compute x's `Result` with x in-scope

env/x

…	…
x	CIRCULAR-ERROR

Running **`bind/rec`**, recursive environment items

```
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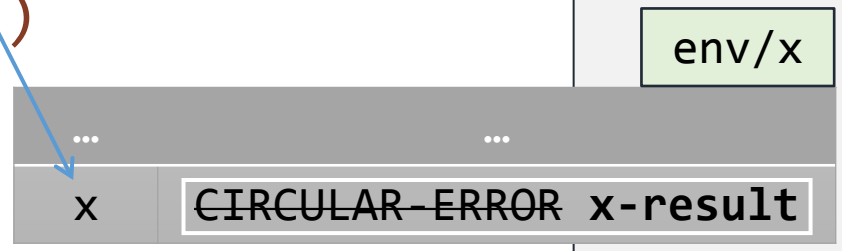
(define (run p)
  (define (run/e p env)
    (match p    …
     [(brec x e body)
      (define placeholder (box CIRCULAR-ERROR)
      (define env/x (env-add env x placeholder)
      (define x-result (run/env e env/x)
      (set-box! placeholder x-result)
      (run/env body env/x)]
                …  ))
  (run/e p INIT-ENV ))
```

Close the (circular data structure) loop, with **mutation!**

Explicitly **mutate** mutable box



Running **`bind/rec`**, recursive environment items

CS450JSLANG

```
(bind/rec
 [fac
  (fn (n)
    (iffy n
          (* n (fac (- n 1)))
          1))]
  (fac 5)) ; => 120
```

```
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       (define x-result (run/env e env/x))
       (set-box! placeholder x-result)
       (run/env body env/x)]
                    …  ))
  (run/e p INIT-ENV ))
```

Compute body with x in-scope

env/x

…	…
x	~~CIRCULAR-ERROR~~ **x-result**

HW 9 Preview: Recursion!

Use “CS450JS LANG”! … to write recursive programs:

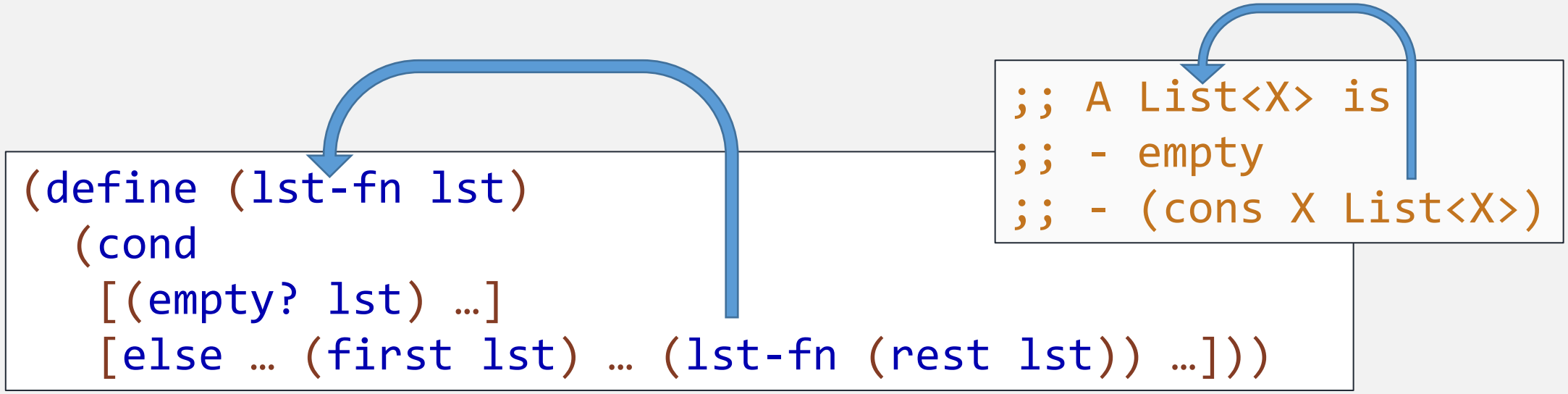
- `fac` (factorial)
- `filt` (filter)
- `qsort` (functional quicksort)
- `gcd`
- `sierpinski` (fractal)

(Extra primitives will be added to `INIT-ENV`, ask if you need more)

- Look it up if you don’t know any of these
  - Using any resources, e.g., ChatGPT, Co-pilot, is allowed
  - (still can’t submit else’s hw, obv)

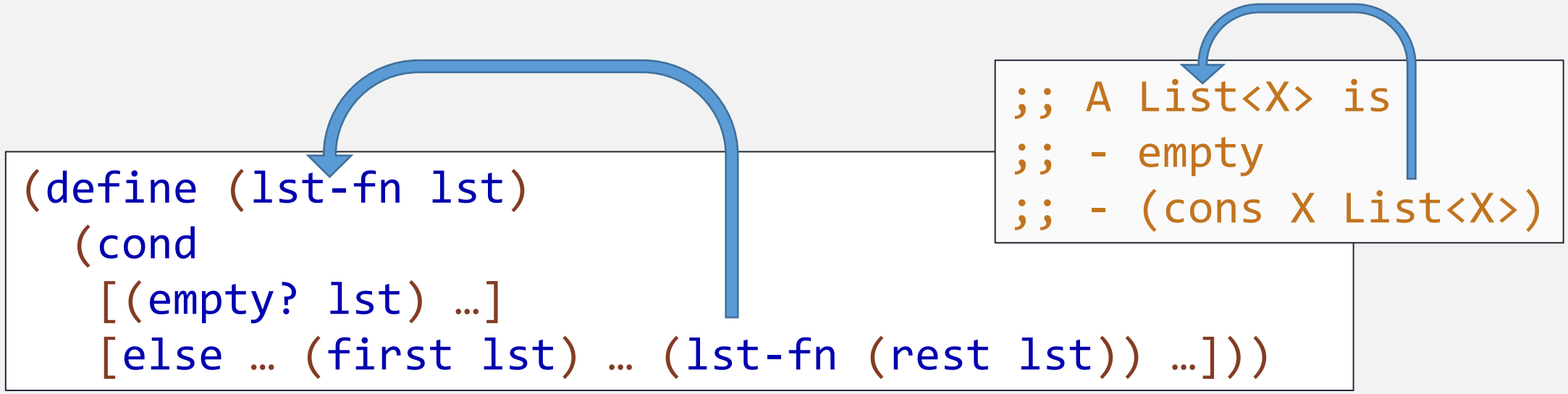
Recursion review

- **Most recursion is structural** (comes from **data definitions**)**!**



A Different Kind of Recursion!

- **Not all recursion is structural** (comes from **data definitions**)**!**



A Different Kind of Recursion!

- **Not all recursion is structural** (comes from **data definitions**)!

```
;; gcd : Nat Nat -> Nat
;; computes greatest common divisor, using Euclid's algorithm
;; termination argument:
;; m is halved (at least) ev                    ia modulo fn)
(define (gcd n m)
  (if (= m 0)
      n
      (gcd m (modulo n m))))
```

What template is this following??

A Different Kind of Recursion!

- **Non-structural recursion** (doesn't come from **data definitions** is called **generative recursion**
- no template, but requires **Termination Argument**
  - Explains why the function terminates!

```
;; gcd : Nat Nat -> Nat
;; computes greatest common divisor, using Euclid's algorithm
;; termination argument:
;; m is halved (at least) every iteration (via modulo fn)
(define (gcd n m)
  (if (= m 0)
      n
      (gcd m (modulo n m))))
```

Recursive call must be on "smaller" version of the problem

HW 9 Preview: Recursion!

Use “CS450JS LANG”! … to write recursive programs:

- `fac` (factorial)
- `filt` (filter)
- `qsort` (functional quicksort)
- `gcd`
- `sierpinski` (fractal)

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- Look it up if you don’t know any of these
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- Repo: **`cs450f23/lecture25-inclass`**
- File: **`recursive-examples-`**<*your last name*>**`.rkt`**

In-class Coding 12/4: recursion

Use “CS450JS LANG”! … to write recursive programs:

- `fac` (factorial)
- `filt` (filter)
- `qsort` (functional quicksort)
- `gcd`
- `sierpinski` (fractal)

(Extra primitives will be added to `INIT-ENV`, ask if you need more)

- Look it up if you don’t know any of these
  - Using any resources, e.g., ChatGPT, Co-pilot, is allowed
  - (still can’t submit else’s hw, obv)

No More Quizzes!

but push your in-class work to:
Repo: **`cs450f23/lecture25-inclass`**